

Copula model selection using image processing

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Overview

- 1 Copula model selection
- 2 Image processing approach
- 3 Experiments
- 4 Concluding remarks and future work

Copula model selection and some commonly used criteria

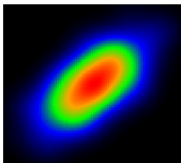
Copulas are widely used for the modelling of dependent risks, with extensive applications in actuarial and financial risk management.

Choosing a suitable copula family, when multivariate datasets are of small to moderate size, is a non-trivial task.

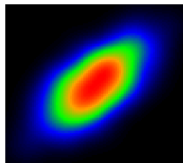
Some commonly used criteria:

- AIC,
- BIC,
- Cross-validated log-likelihood criterion,
- Cramer-von Mises statistic.

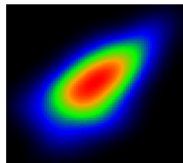
Image patterns for different models



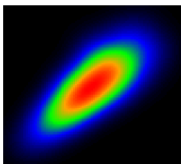
(a) Gaussian



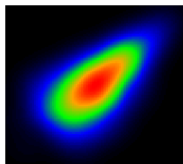
(b) t



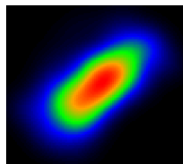
(c) Gumbel



(d) Clayton



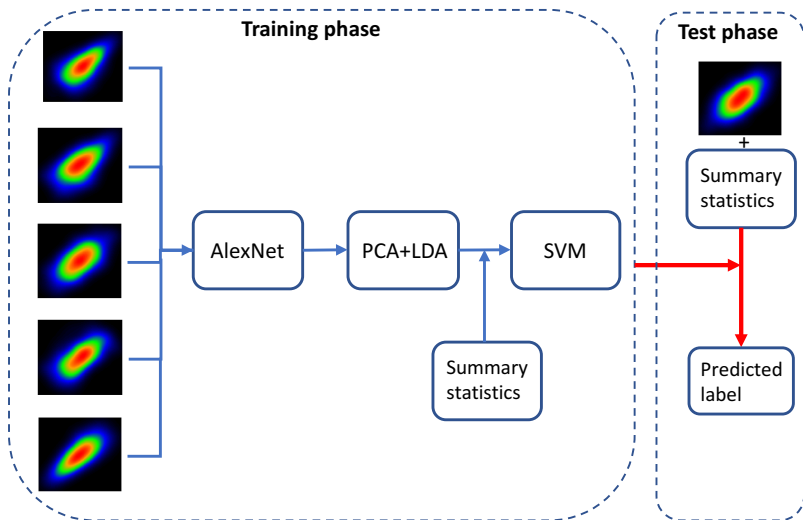
(e) Joe



(f) Frank

The workflow of the image processing approach

A classification task:



Dealing with negative correlations

Step 1 If the estimated correlation is negative, rotate the image by 90 degrees.

Step 2 If the skewness statistic is negative, rotate the image by 180 degrees.

The rotation steps are applied to all images before the training phase.

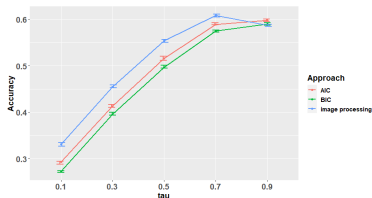
Assessment criterion

If the rotation step is correct **and** the classification is correct, the image is treated as correctly classified.

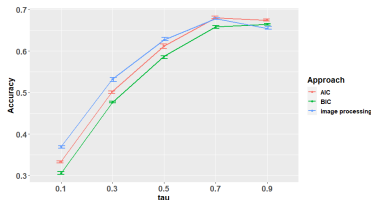
Experiments

We consider **6 copula models** (Gaussian, t, Gumbel, Clayton, Joe and Frank) and **all their rotations**.

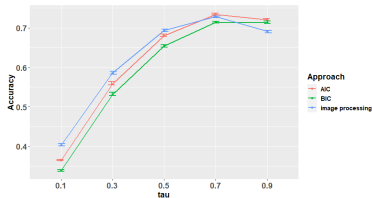
Experiment results: train models with fixed sample size and correlation



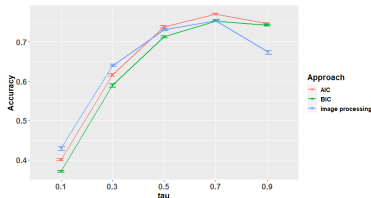
(a) $n = 100$



(b) $n = 150$

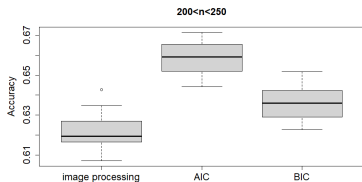
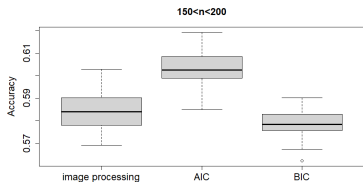
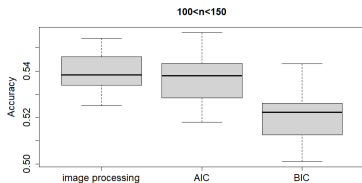
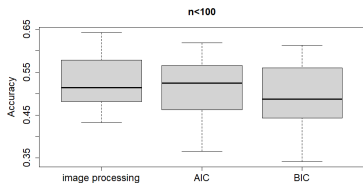


(c) $n = 200$



(d) $n = 250$

Experiment results: train one model with variable sample size and correlation



Concluding remarks and future work

- For small sample size and small correlation: the image processing approach can provide superior classification performance over AIC and BIC.
- For large sample size and large correlation: AIC dominates.
- Future work: a combination of image processing and AIC to provide good classification performance for all values of sample size and correlation.