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# The use of denoising autoencoders for categorical and continuous variables

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joint work with Łukasz Delong<sup>1,2</sup>

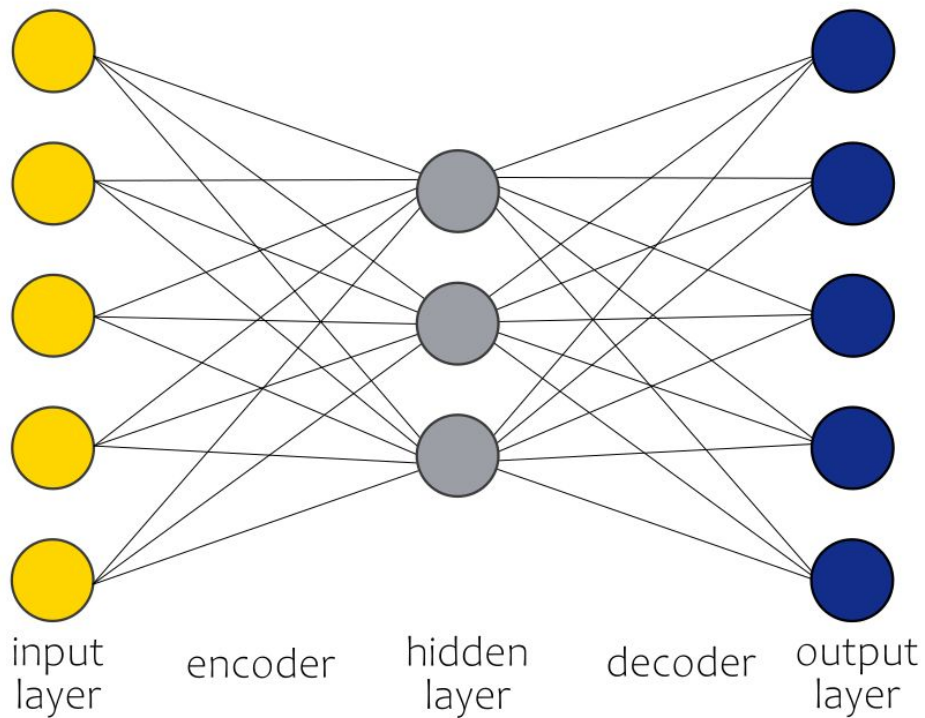
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Test autoencoders on categorical variables, until now Entity Embedding has been used in the actuarial field.

# Autoencoders



# Benefits of using autoencoders

Erhan, Dumitru and Manzagol, Pierre-Antoine and Bengio, Y. and Bengio, S. and Vincent, Pascal . (2009). *The Difficulty of Training Deep Architectures and the Effect of Unsupervised Pre-Training*. Twelfth International Conference on Artificial Intelligence and Statistics

Vincent, Pascal and Larochelle, Hugo and Lajoie, Isabelle and Bengio, Y. and Manzagol, Pierre-Antoine. (2008). *Extracting and composing robust features with denoising autoencoders*. In ICML 2008: Proceedings of the Twenty-fifth International Conference on Machine Learning

Vincent, Pascal and Larochelle, Hugo and Lajoie, Isabelle and Bengio, Y. and Manzagol, Pierre-Antoine. (2010). *Stacked Denoising Autoencoders: Learning Useful Representations in a Deep Network with a Local Denoising Criterion.*, Journal of Machine Learning Research

# Autoencoders for categorical variables

- autoencoder softmax all
- autoencoder softmax per variable

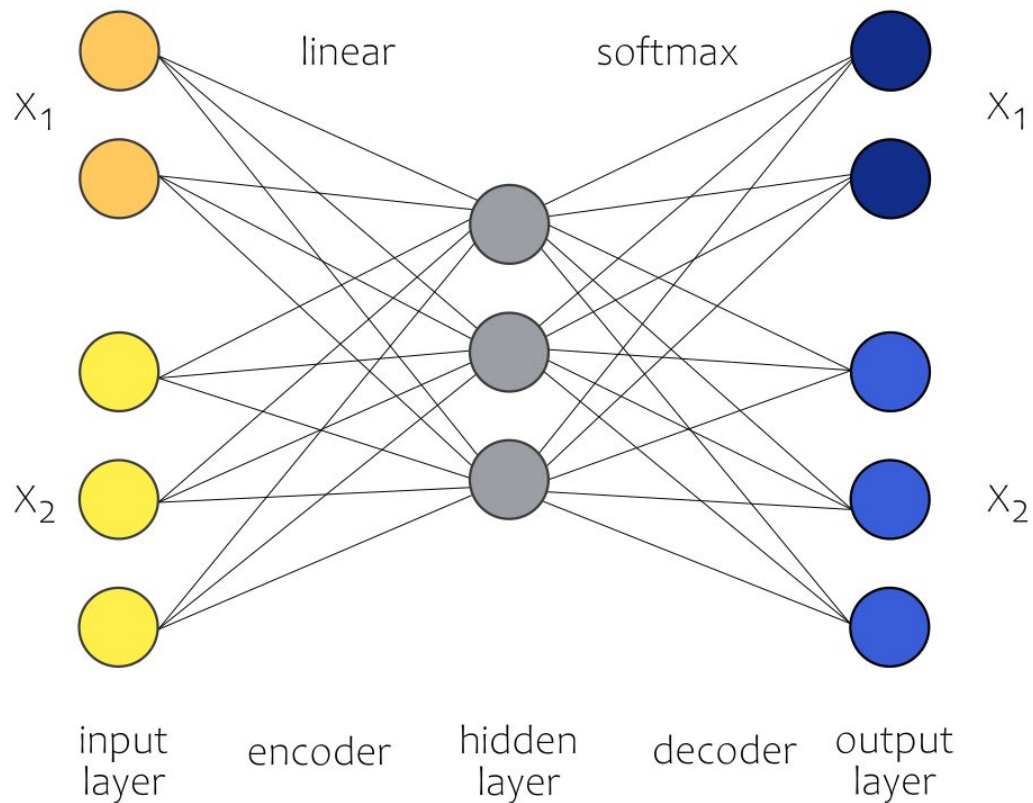
Categorical variables should be one-hot encoded before constructing the autoencoder.

We noise all observations and one, two or three randomly selected columns per observation.

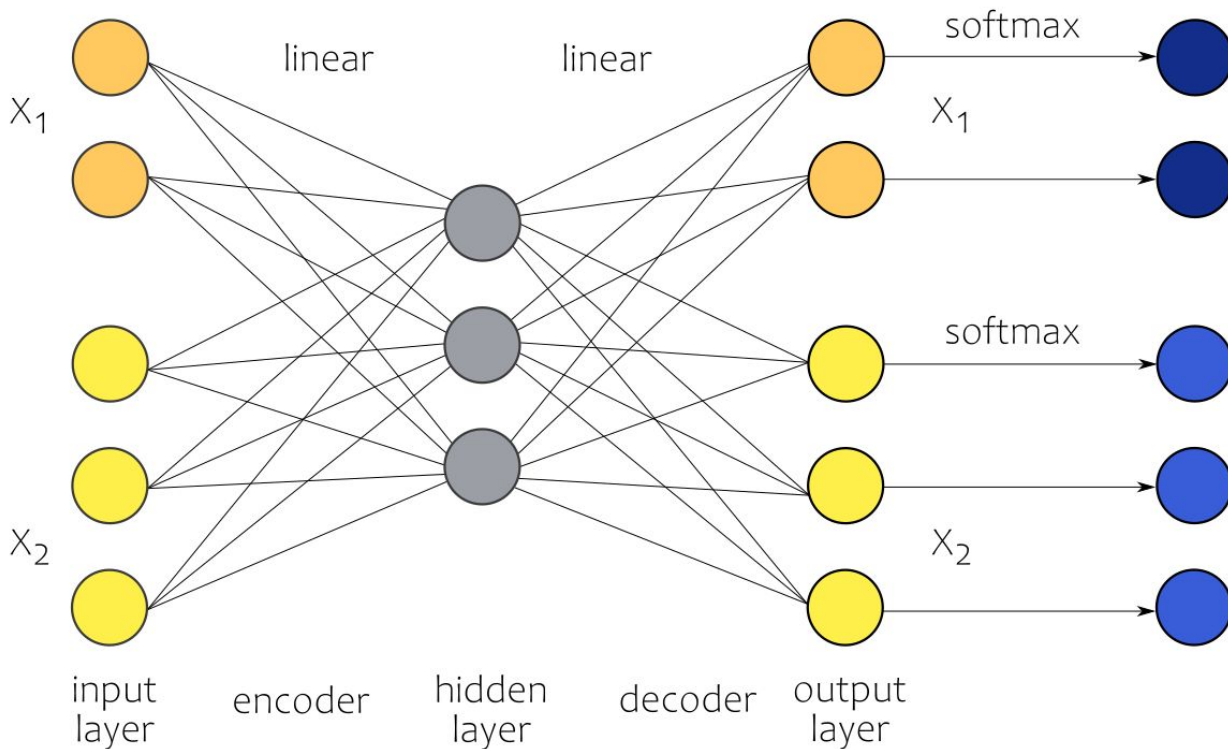
Each autoencoders we consider with noise. Types of noise:

- zeros                      00100000 → 00000000
- sample                     00100000 → 00000010

# Autoencoder softmax all



# Autoencoder softmax per variable





# Autoencoders for numerical variables

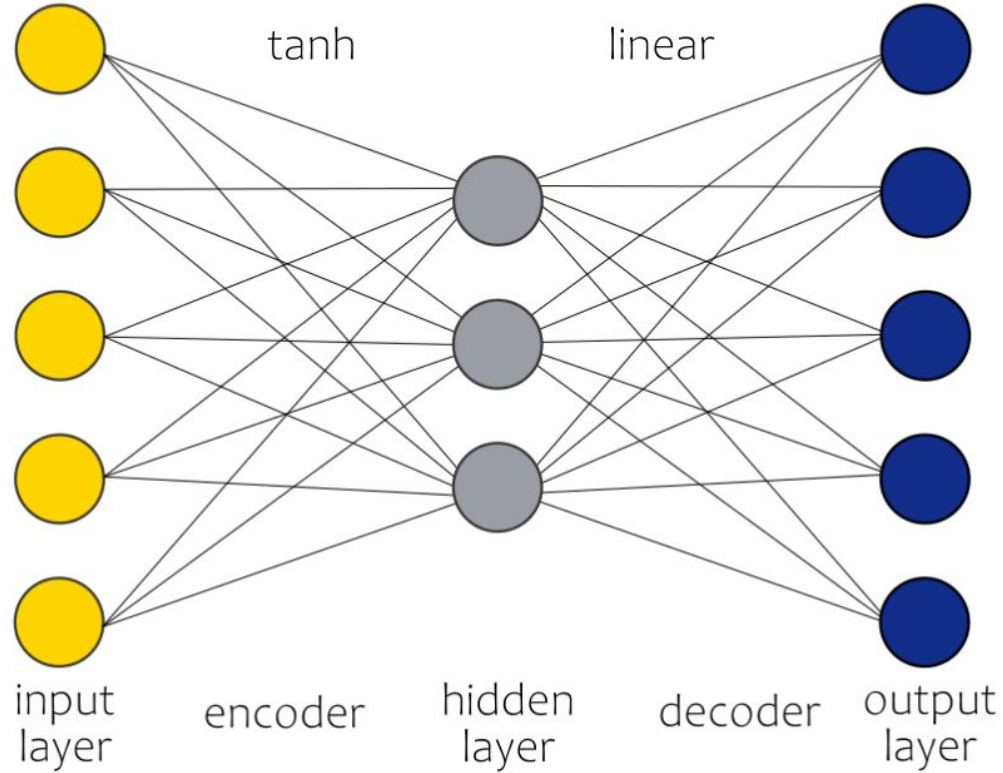
- autoencoder MSE

We noise all observations and one, two or three randomly selected columns per observation.

Each autoencoders we consider with noise. Types of noise:

- const - change value to zero
- sigma - change value to random value from normal distribution with expected value equal to the value from dataset and variance equal sigma square

# Autoencoder for numerical variables



# Dataset and experiments

*Dataset:* freMTPL2freq, select 100k observations by stratification

*Categorical variable:* Area, VehPower, VehAge, DrivAge, VehBrand, Region

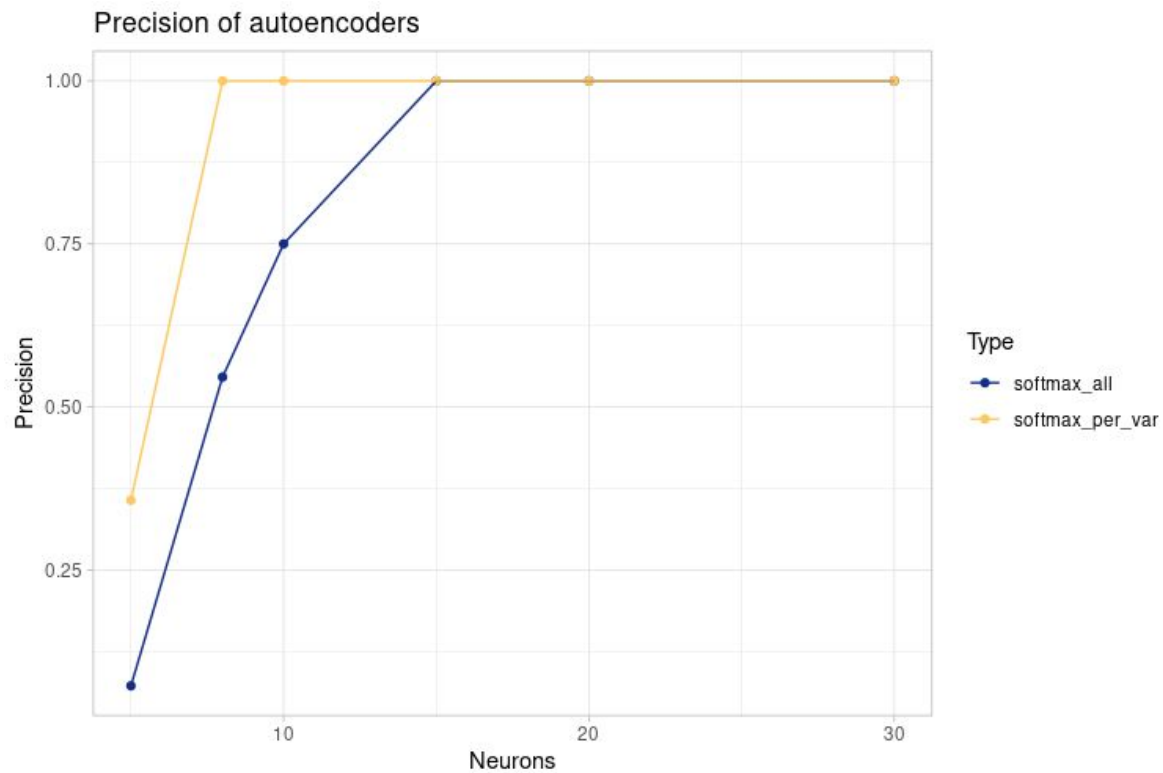
*Binary variable:* VehGas

*Numerical variable:* BonusMalus, Density (log), Min-Max scaler

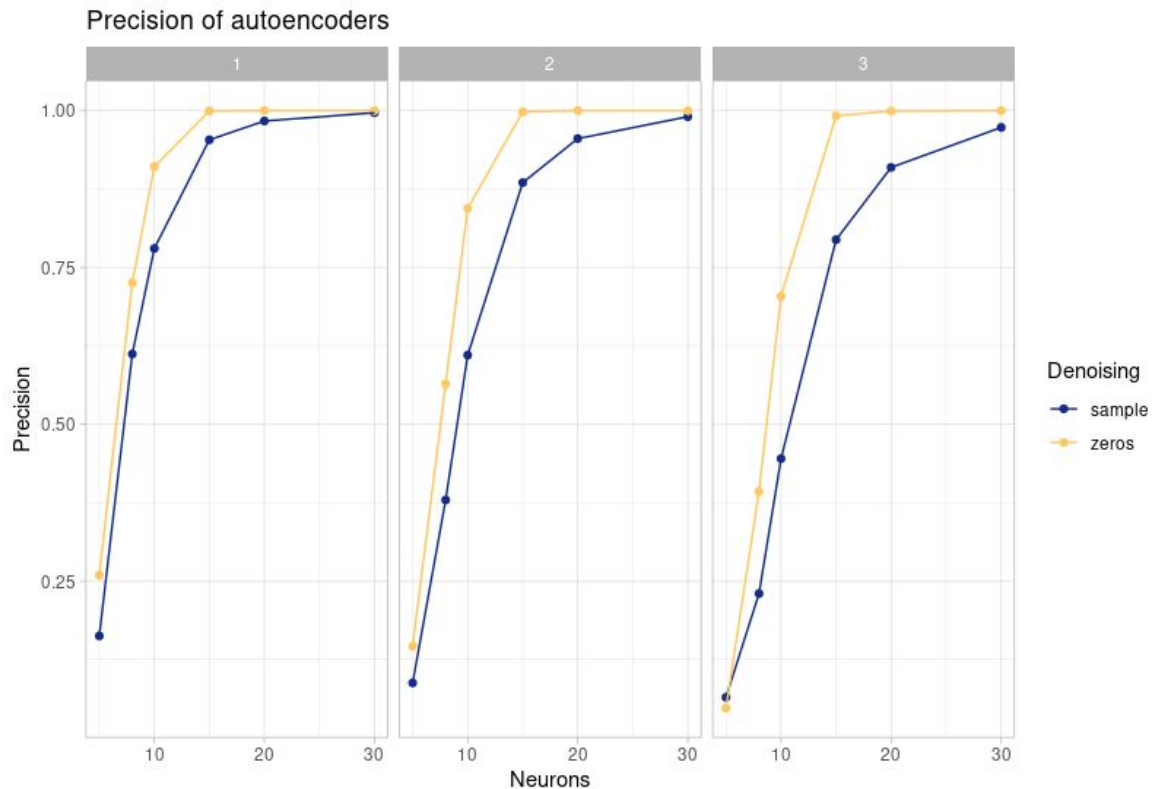
Experiments with autoencoder for categorical variables:

Parameter	Value
neurons	5, 8, 10, 15, 20, 30
epochs	500
batch size	1000
learning rate	0.001
min delta	0
patience	15
noise	zeros, sample

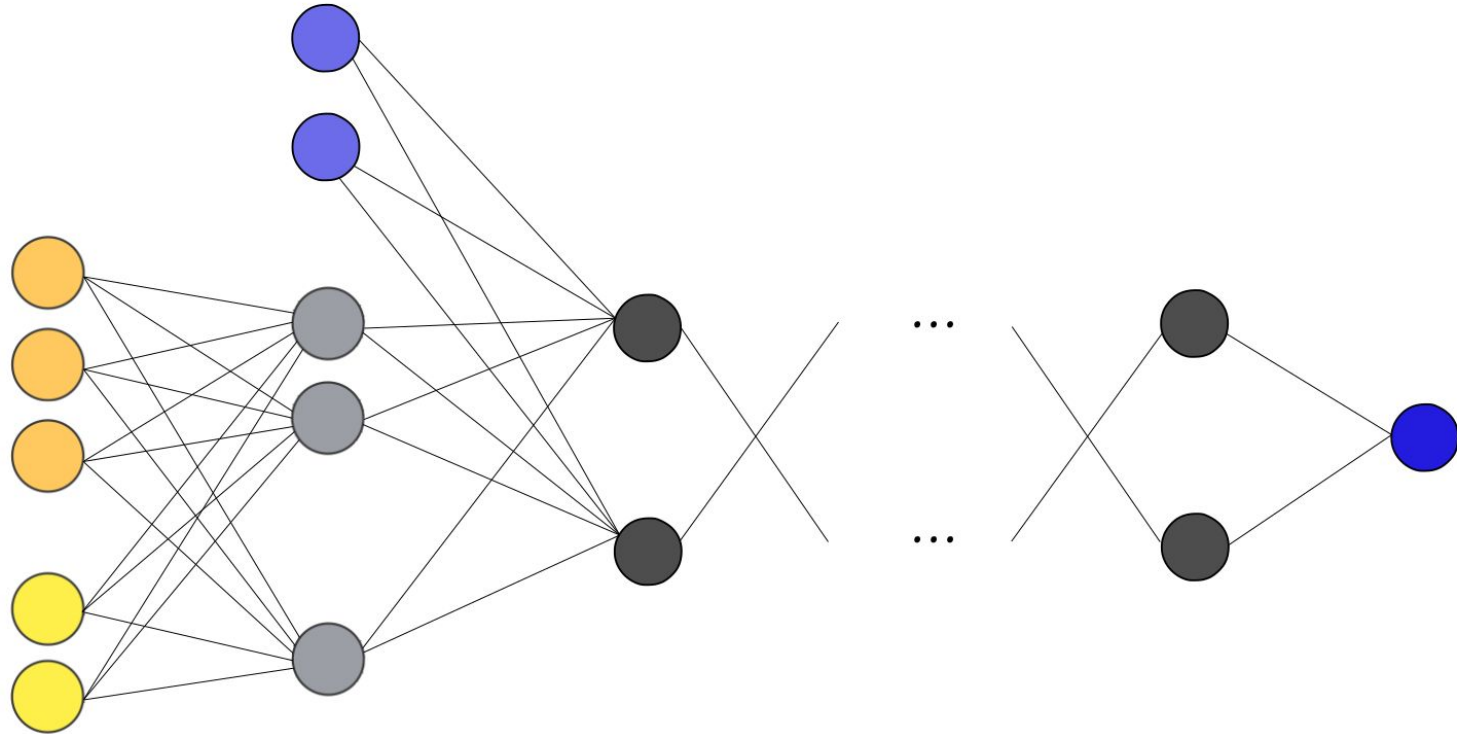
# Results for autoencoders



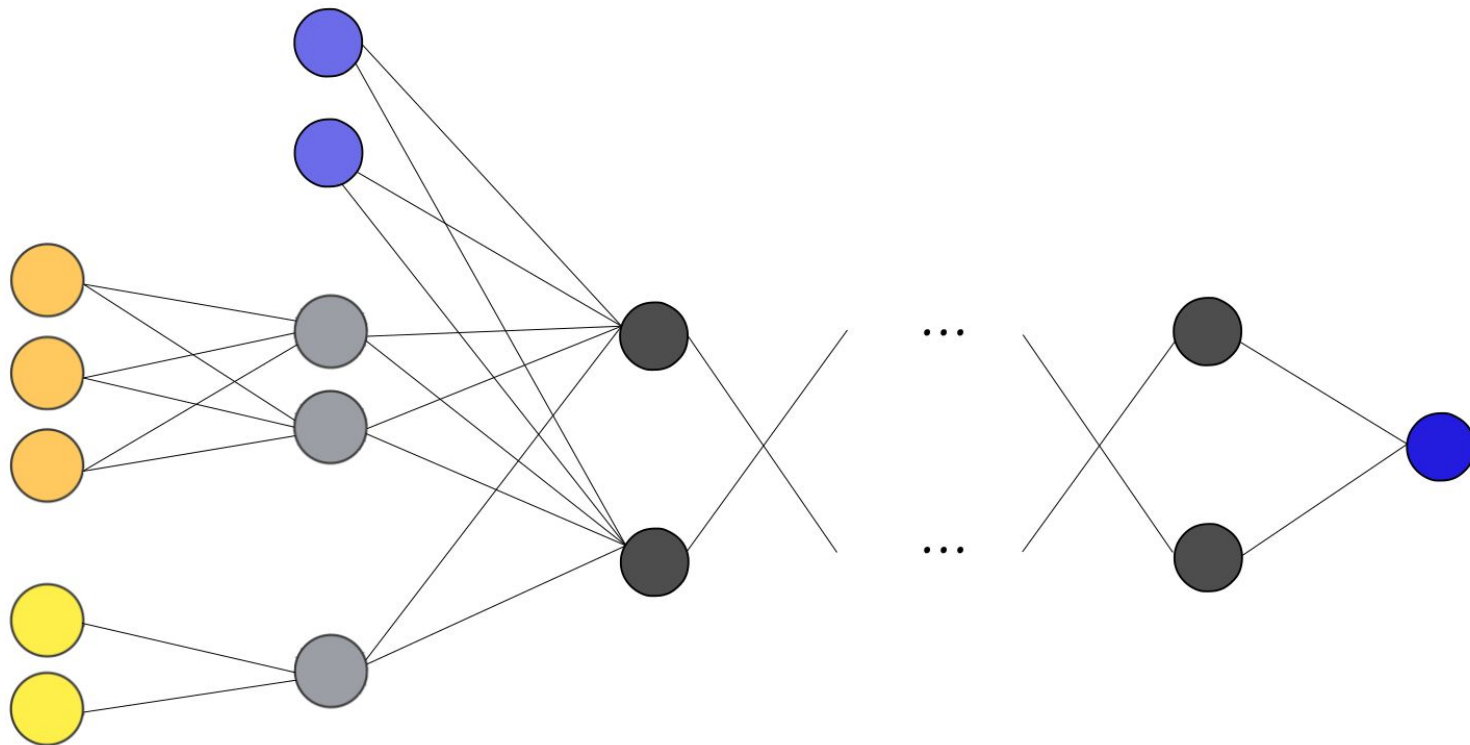
# Results for autoencoder softmax per variable with denoising



# Neural Networks with autoencoders



# Neural Networks with Entity Embedding



# Experiments

With weight from autoencoder		
1 AE	epochs	15, 50, 100, 200, 300
	learning rate	$5 * 10^{-5}$ , $5 * 10^{-4}$ , $5 * 10^{-3}$
	denoising	sample, zeros
	cols	1, 2, 3
2 AE	denoising	const, sigma
	sigma/feat noise	0, 0.1, 0.25, 0.5 / 0.1, 0.3, 0.5
	epochs	15, 50, 100, 200, 300
	learning rate	$5 * 10^{-5}$ , $5 * 10^{-4}$ , $5 * 10^{-3}$
Neural Network	number layer	1, 3
	neurons layer	[20], [30], [50],[30, 30, 30], [30, 20, 10], [20, 15, 10]
	learning rate	$10^{-4}$ , $10^{-3}$ , $10^{-2}$

Without weight from autoencoder	
number layer	1, 3
neurons layer	[20], [30], [50],[30, 30, 30], [30, 20, 10], [20, 15, 10]
learning rate	$10^{-4}$ , $10^{-3}$ , $10^{-2}$

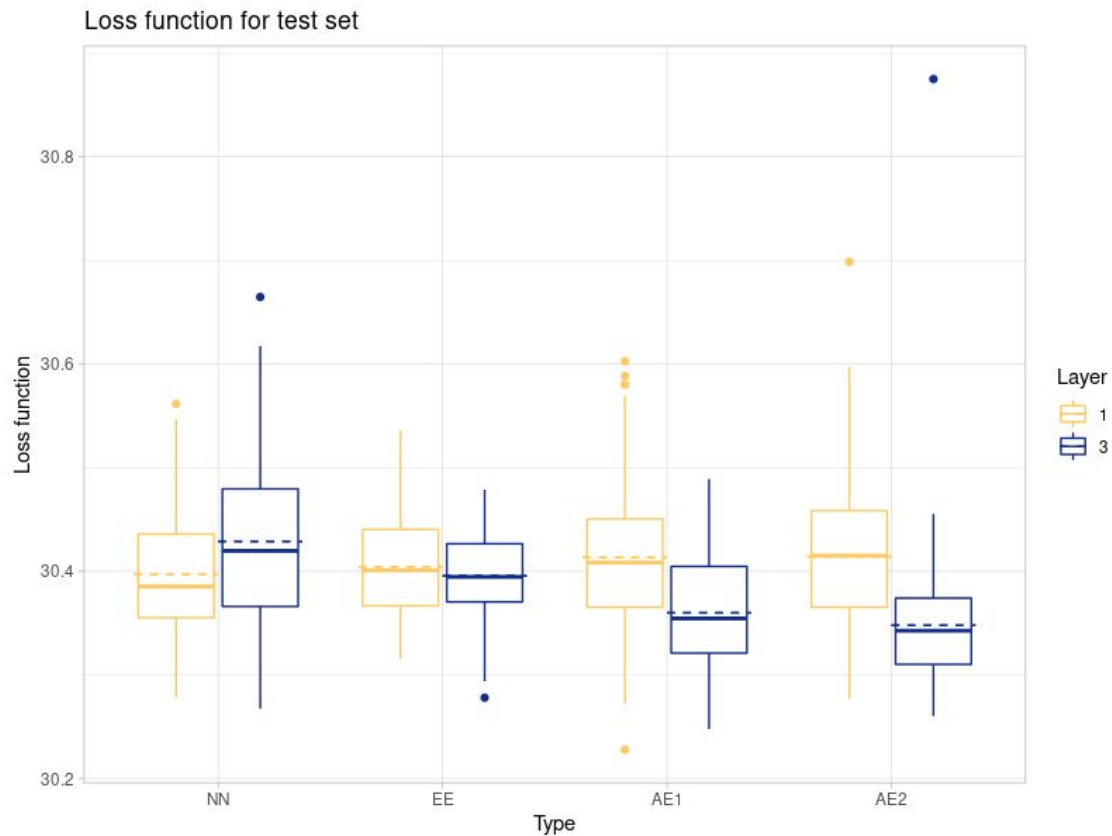
Entity Embedding	
number layer	1, 3
neurons layer	[47], [57], [77], [25, 20, 11], [35, 24, 10], [33, 32, 32]
learning rate	$10^{-4}$ , $10^{-3}$ , $10^{-2}$



# Models chosen with 5 fold cv

neurons number	neurons_layer	number layer	learning rate AE	learinig rate	epochs	type	test
8	[20]	1	0.00005	0.01	100	2 AE	31,088
8	[50, 35, 20]	3	0.005	0.0001	15	2 AE	31,043
8	[20, 15, 10]	3	0.005	0.0001	200	2 AE	31,061
8	[50]	1	0.005	0.01	50	2 AE	31,100
8	[20]	1	0.00005	0.0001	15	1 AE	31,081
8	[20]	1	0.005	0.01	200	1 AE	31,081
8	[50]	1	0.0005	0.01	100	1 AE	31,083
8	[20, 15, 10]	3	0.0005	0.0001	100	1 AE	31,069
8	[50, 35, 20]	3	0.005	0.0001	15	1 AE	31,056
8	[50, 35, 20]	3	0.005	0.001	15	1 AE	31,061
8	[25, 20, 11]	3		0.001		EE	31,104
8	[50, 35, 20]	3		0.0001		NN	31,127
8	[30]	1		0.001		NN	31,097
8	[57]	1		0.01		EE	31,124

# Results on test set - loss functions



# Results on test set - loss functions

## One layer

	EE	NN	AE1	AE2
1st Q	30,370	30,360	30,370	30,370
<b>mean</b>	<b>30,400</b>	<b>30,400</b>	<b>30,410</b>	<b>30,410</b>
3rd Q	30,440	30,440	30,450	30,460
sd	0,052	0,057	0,070	0,072

## Three layer

	EE	NN	AE1	AE2
1st Q	30,370	30,370	30,320	30,310
<b>mean</b>	<b>30,400</b>	<b>30,430</b>	<b>30,360</b>	<b>30,350</b>
3rd Q	30,430	30,480	30,400	30,370
sd	0,040	0,083	0,053	0,068

# Results on test set - claim intensities

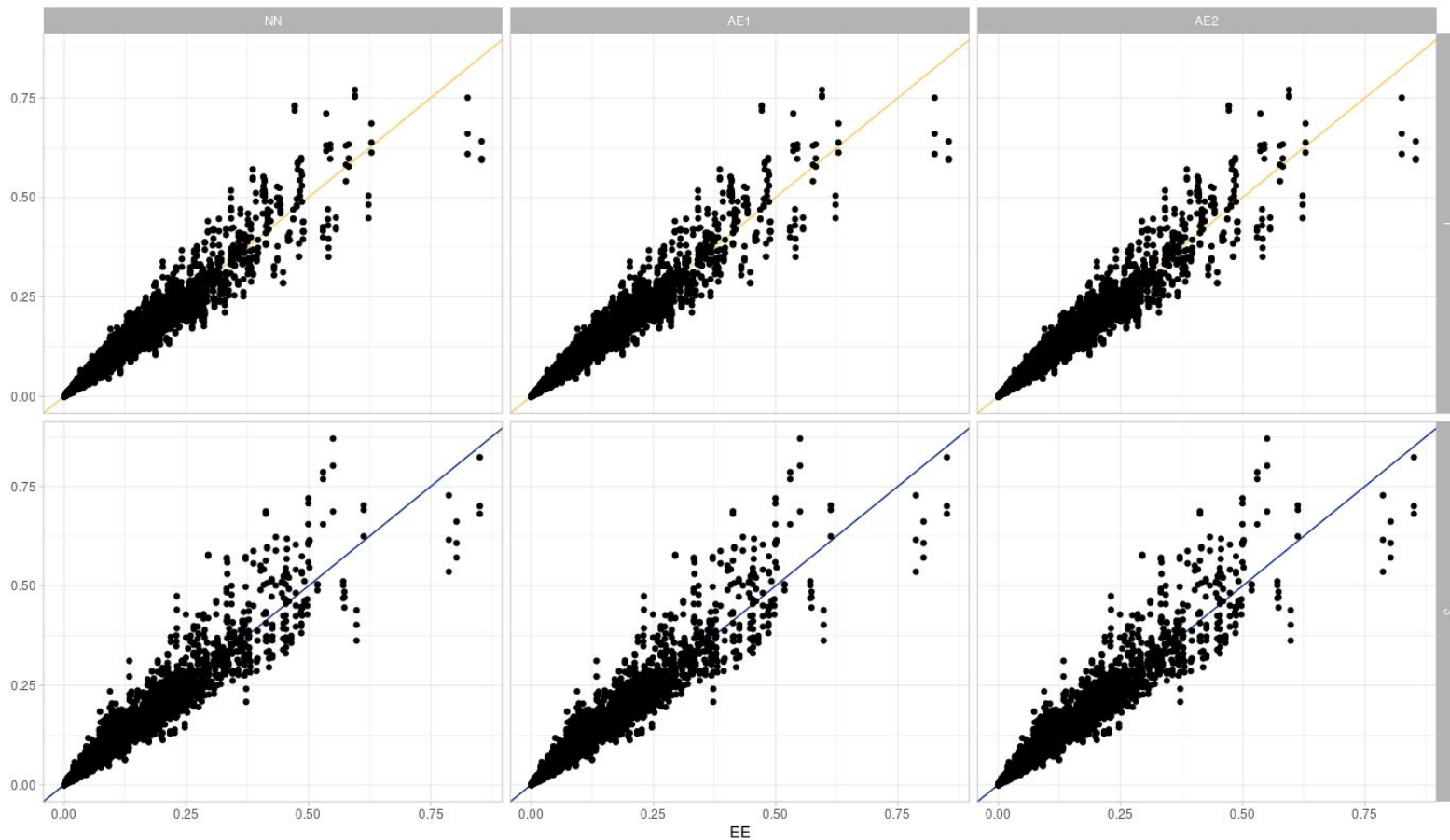
One layer

	NN	EE	AE1	AE2
1st Q	4,996	4,923	4,948	4,907
<b>mean</b>	<b>5,071</b>	<b>5,044</b>	<b>5,086</b>	<b>5,063</b>
3rd Q	5,157	5,17	5,236	5,178
sd	0,102	0,170	0,189	0,224
<b>y mean</b>	<b>5,105</b>	<b>5,105</b>	<b>5,105</b>	<b>5,105</b>

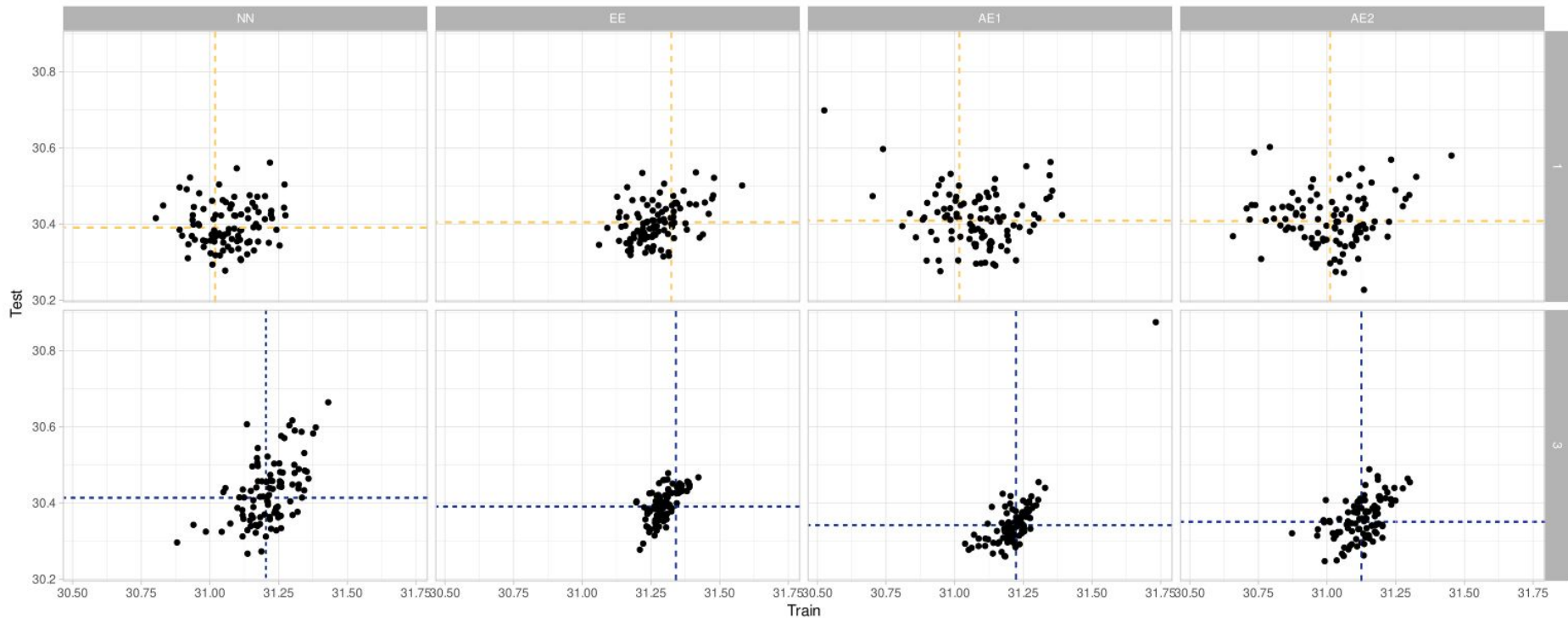
Three layer

	NN	EE	AE1	AE2
1st Q	5,099	4,981	5,141	5,234
<b>mean</b>	<b>5,149</b>	<b>5,054</b>	<b>5,183</b>	<b>5,262</b>
3rd Q	5,207	5,142	5,221	5,288
sd	0,068	0,114	0,060	0,039
<b>y mean</b>	<b>5,105</b>	<b>5,105</b>	<b>5,105</b>	<b>5,105</b>

# Results on test set - claim intensities



# Results on train and test sets - loss functions



# What improvement comes with adding autoencoder?

AE	Loss function	Difference
0	30,408	
1	30,380	0,028
2	30,348	0,032

# What improvement comes with adding autoencoder?

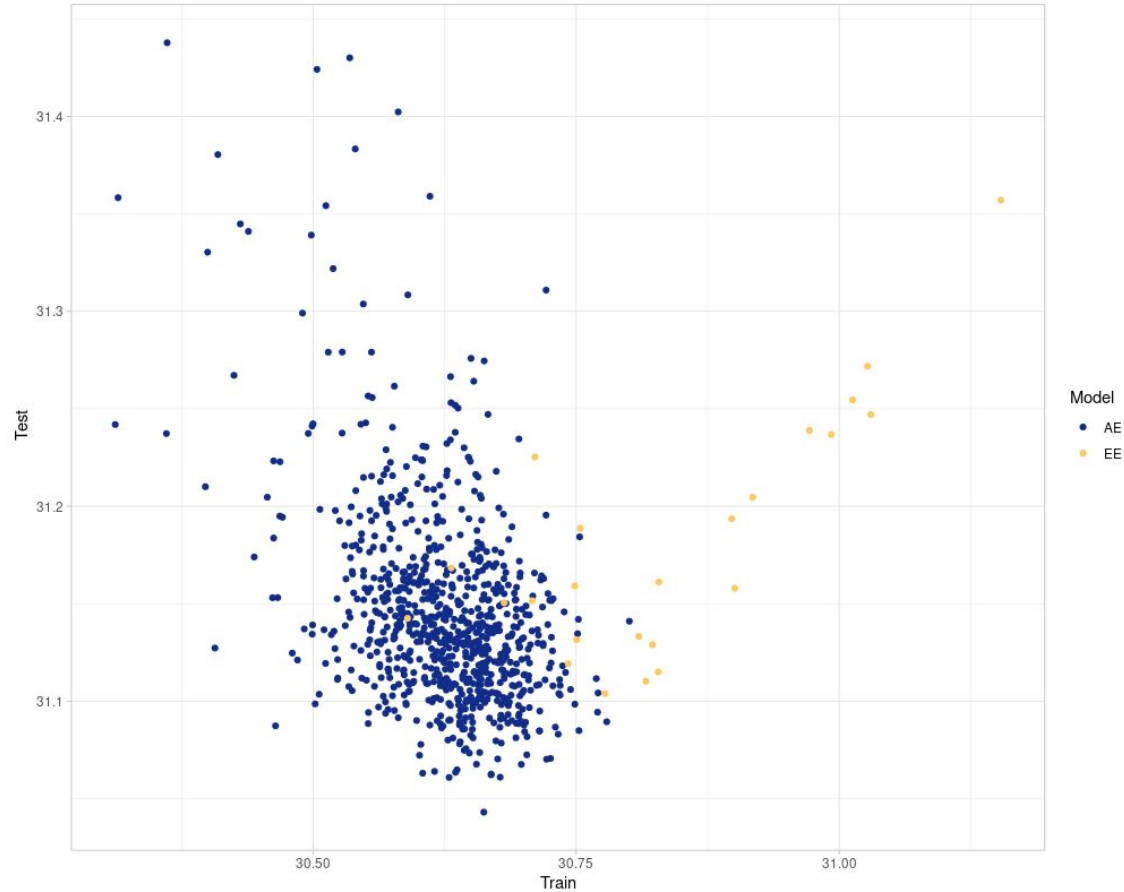
AE	Scaled weights	Loss function	Difference
1	No	30,674	
1	Yes	30,380	0,294



# What improvement comes with adding autoencoder?

AE	Scaled weights	Neurons	Loss function	Difference
2	Yes	8	30,348	
2	Yes	11	30,336	0,012

# Results on train and test sets - loss functions



# Bibliography

*Wuthrich, Mario. (2019). From Generalized Linear Models to Neural Networks, and Back. SSRN Electronic Journal.*

*Erhan, Dumitru and Manzagol, Pierre-Antoine and Bengio, Y. and Bengio, S. and Vincent, Pascal . (2009). The Difficulty of Training Deep Architectures and the Effect of Unsupervised Pre-Training. Twelfth International Conference on Artificial Intelligence and Statistics*


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Thank you for your attention!