



- News
- Events
- Conferences
- Cass Talks

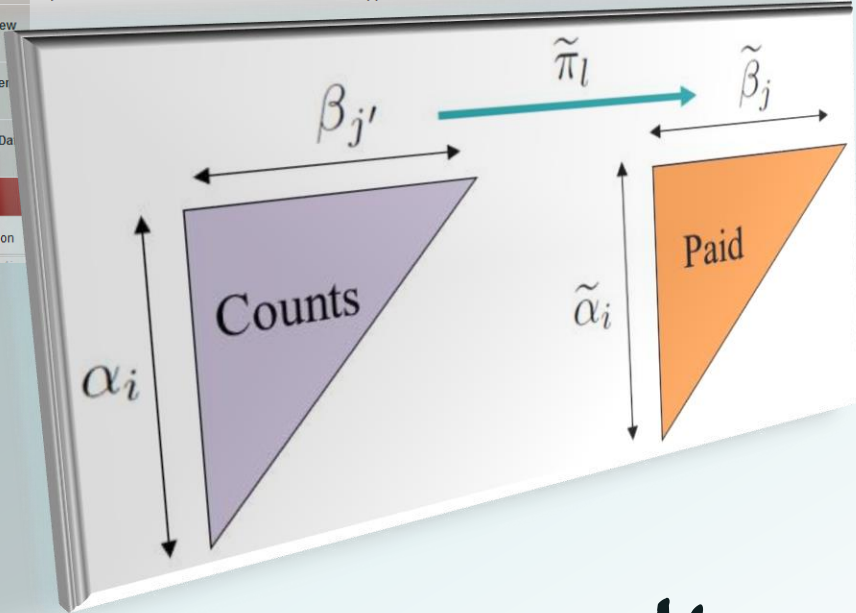
Conferences

R in Insurance

The first conference on R in Insurance will be held on Monday 15 July 2013 at Cass Business School in London, UK.

The intended audience of the conference includes both academics and practitioners who are active or interested in the applications of R in Insurance.

- Econometrics, Energy and Finance
- EMG Workshop on International Capital Flows and the Global Economy
- Initial Public Offerings: New Challenges Workshop
- Cass Real Estate Conference 2013
- 19th International Panel Discussion Conference
- R in Insurance
- Talk Proposal Submission



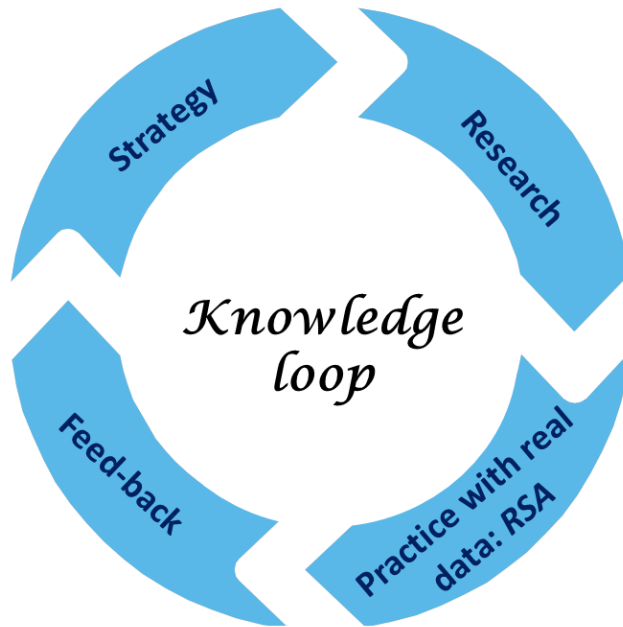
RBNS preserving –
A new method in
the DCL
-package



Munir Hiaab
Carolin Margraf
Maria Dolores Martinez-Miranda
Jens Perch Nielsen



Background



2010 Including Count Data in Claims Reserving

2011 Cash flow simulation for a model of outstanding liabilities based on claim amounts and claim numbers

2012 Double Chain Ladder



2012 Statistical modelling and forecasting in Non-life insurance

2013 Double Chain Ladder and Bornhuetter-Ferguson


2013 Double Chain Ladder, Claims Development Inflation and Zero Claims

2014 RBNS preserving Double Chain Ladder (submitted)



Our aim: a package implementing recent research developments

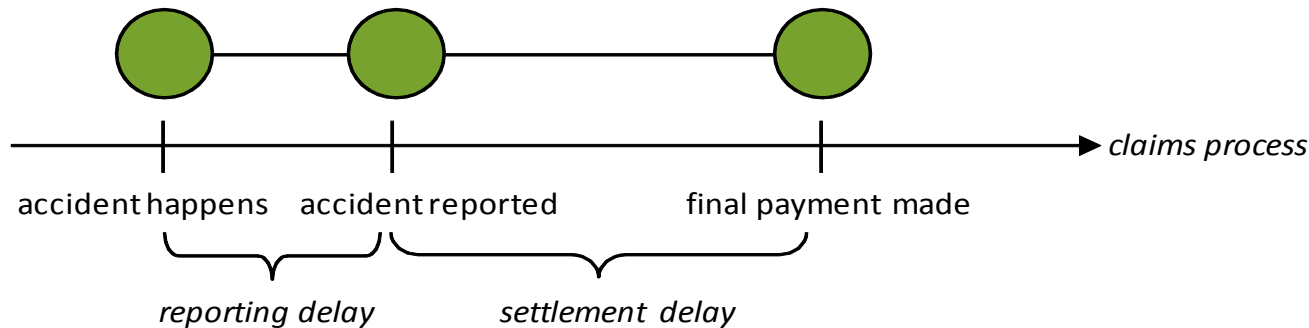


- (1) Introducing the problem: stochastic reserving
- (2) Motivating a statistical model for stochastic reserving: the [Double Chain Ladder Model](#)
- (3) Incorporating expert knowledge: [RBNS preserving Double Chain Ladder](#)
- (4) The -Package: [DCL](#)



The problem: the claims reserving exercise

The life of an individual claim in the general claims process:



Incurred but not reported, **IBNR**

Reported but not settled, **RBNS**

Reported and paid



The problem: the claims reserving exercise

- The objectives:
 - ✓ How large **future claims payments** are likely to be.
 - ✓ The **timing** of future claim payments.
 - ✓ The **distribution** of possible outcomes: future **cash-flows**.



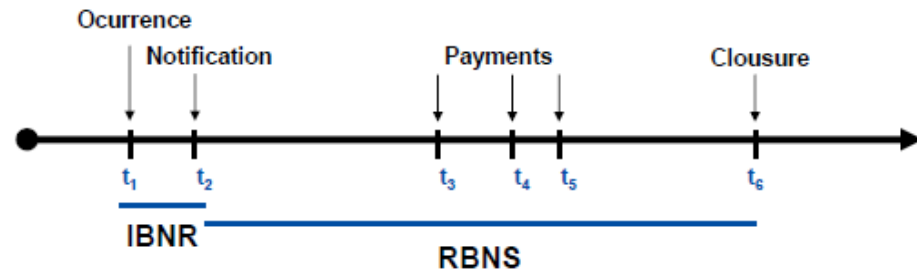
Framework: Double Chain Ladder

What is Double Chain Ladder?

A firm **statistical model** which **breaks down the chain ladder estimates into individual components**.

Why?

- ✓ **Connection with classical reserving (tacit knowledge)**
- ✓ **RBNS** and **IBNR** claims
- ✓ The distribution: **full cash-flow**



IBNR: Incurred But Not Reported

RBNS: Reported But Not Settled

Reserve = IBNR + RBNS

What is required? It works on **run-off triangles**

(adding **expert knowledge** if available).



The modelled data: two run-off triangles

We model annual/quarterly run-off triangles:

- ❑ Incremental aggregated payments (paid triangle).
- ❑ Incremental aggregated counts data, which is assumed to have fully run off.

DEVELOPMENT →

Payment data

	1	2	3	4	5	6	7
A							
C							
I							
D							
E							
N							
T							

REPORTING →

Counts data

	1	2	3	4	5	6	7
A							
C							
I							
D							
E							
N							
T							



The Double Chain Ladder Model

Parameters involved in the model:

Ultimate claim numbers: α_i

Reporting delay: $\beta_{j'}$

Settlement delay: π_l

Development delay: $\tilde{\beta}_j$

Ultimate payment numbers: $\tilde{\alpha}_i$

Severity:

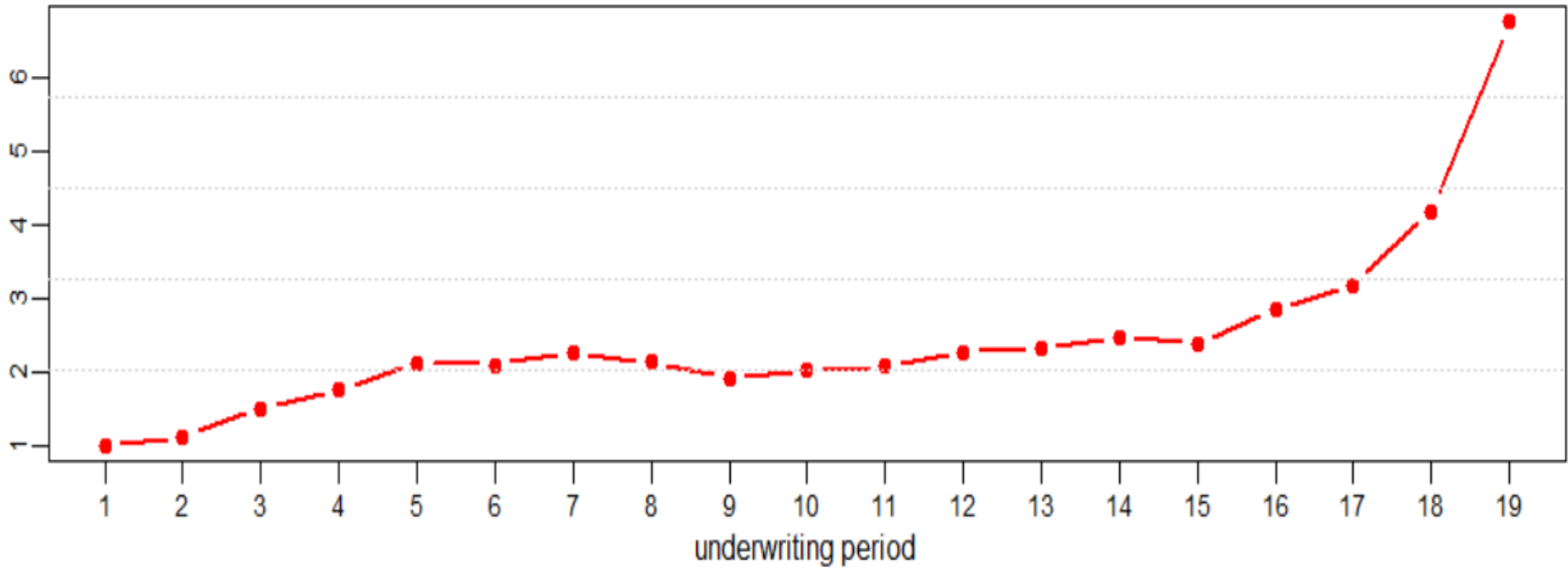
underwriting inflation: γ_i

delay mean dependencies: μ



The Double Chain Ladder Model

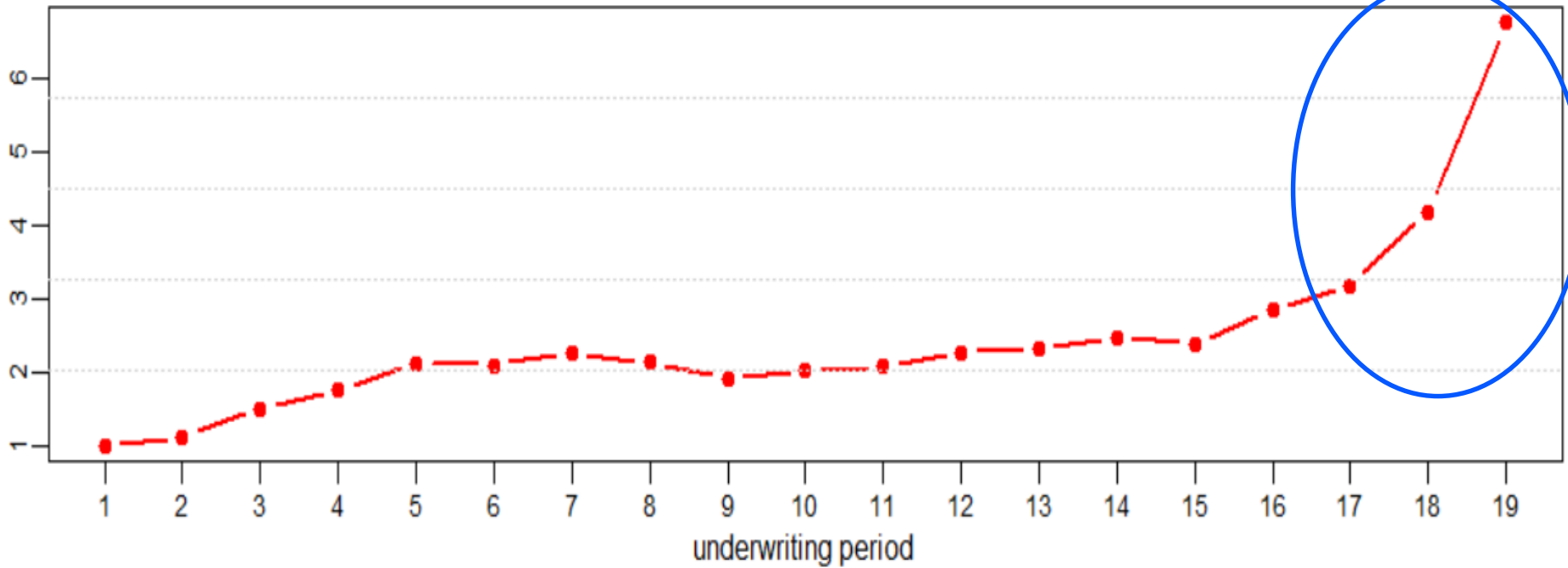
Severity inflation





The Double Chain Ladder Model

Severity inflation





The Double Chain Ladder Model

The reserve per
underwriting year

	reserve	proportion of total reserve
1	0.000000e+00	0.00
2	8.304134e+02	0.00
3	1.073025e+02	0.00
4	8.348906e+02	0.00
5	4.007342e+03	0.00
6	3.141223e+04	0.00
7	1.417988e+05	0.00
8	2.498179e+05	0.00
9	3.595187e+05	0.00
10	3.824873e+05	0.00
11	5.252174e+05	0.00
12	6.315314e+05	0.00
13	9.770538e+05	0.01
14	2.549259e+06	0.01
15	5.449377e+06	0.03
16	1.543851e+07	0.08
17	2.174178e+07	0.11
18	4.445951e+07	0.23
19	9.897470e+07	0.52



The Double Chain Ladder Model

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	reserve	proportion of total reserve
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12	6.315314e+05	0.00
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14	2.549259e+06	0.01
15	5.449377e+06	0.03
16	1.543851e+07	0.08
17	2.174178e+07	0.11
18	4.445951e+07	0.23
19	9.897470e+07	0.52

} = 86% of total reserve



The Double Chain Ladder Model

Summary of the **major drawback** of classical Chain Ladder (and thus the basic Double Chain Ladder method):

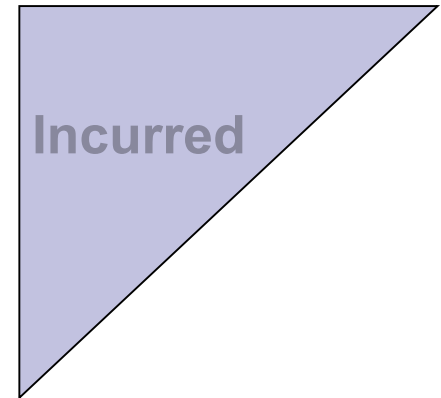
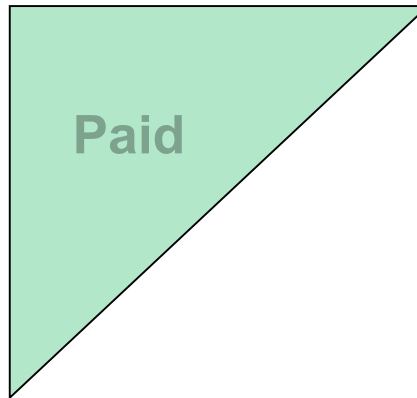
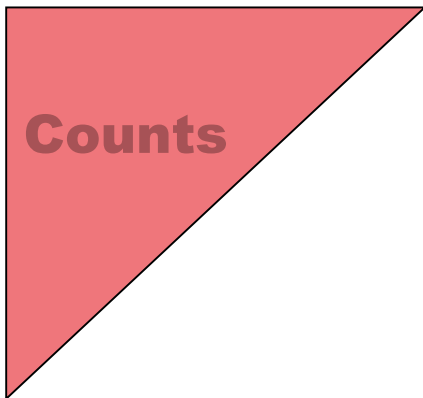
The **lack of sufficient data** in the most recent underwriting years yields to a **severity inflation** estimation being **too instable** and thus not trustable in those most recent years.

Even worse, those most **recent underwriting years** account for the **very major part of the reserve**.



RBNS preserving Double Chain Ladder

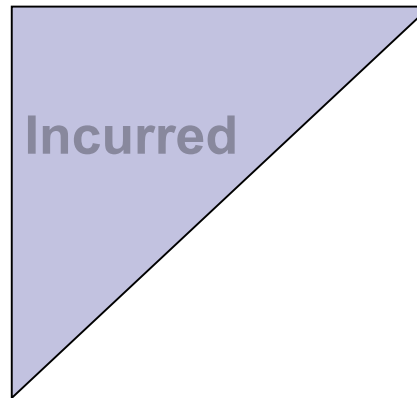
Solution: Incorporate **expert knowledge**





RBNS preserving Double Chain Ladder

The incurred triangle:



- It is **not data**, but a **mixture of data and expert knowledge**
- It contains payments and **case estimates of RBNS claimes**



RBNS preserving Double Chain Ladder

- From the incurred triangle, one can extract the RBNS part estimated by the case department.
- The RBNS case estimates differ from the DCL RBNS estimates



RBNS preserving Double Chain Ladder

	RBNS via DCL	RBNS via case estimates	diff/ultimate
1	0	0	0.0000000000
2	830	0	0.0001524044
3	107	4011	0.0004901895
4	835	-9524	0.0009776366
5	4007	36500	0.0019828617
6	29477	5000	0.0012162334
7	138978	1381	0.0046895341
8	244550	92278	0.0042858333
9	352419	57627	0.0077738288
10	369966	190335	0.0048338207
11	506266	241142	0.0067846411
12	602066	1444	0.0167014947
13	929374	1210062	0.0089660533
14	2453703	2719667	0.0067760876
15	5301958	6123466	0.0190207477
16	15190206	9249185	0.1206529140
17	21248200	13099480	0.1888002860
18	42539709	24828096	0.2802813405
19	74094249	31454377	0.4114369497



RBNS preserving Double Chain Ladder

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9	352419	57627	0.0077738288
10	369966	190335	0.0048338207
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13	929374	1210062	0.0089660533
14	2453703	2719667	0.0067760876
15	5301958	6123466	0.0190207477
16	15190206	9249185	0.1206529140
17	21248200	13099480	0.1888002860
18	42539709	24828096	0.2802813405
19	74094249	31454377	0.4114369497

The values of the severity inflation estimates in the most recent calendar years result in a big difference between DCL and case estimates based RBNS numbers



RBNS preserving Double Chain Ladder

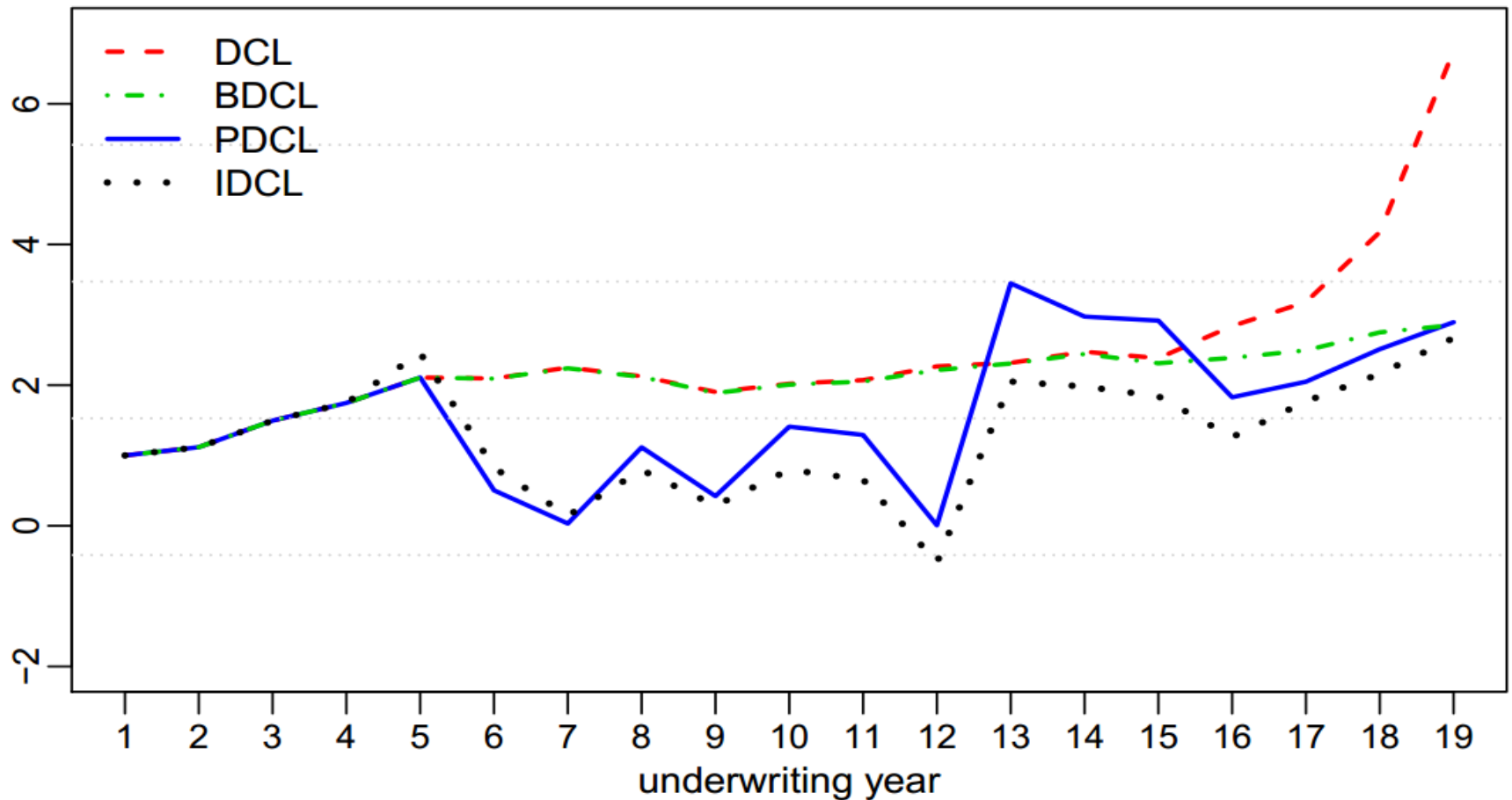
What does RBNS preserving Double Chain Ladder (PDCL) do?

- PDCL preserves the RBNS case estimates.
- Hereby, **the RBNS reserve part is not just replaced by the case estimates.**
- The DCL parameters estimates are adjusted by the use of the incurred triangle.
- Therefore, PDCL estimates the the exact RBNS case estimates but also corrects the IBNR estimates.



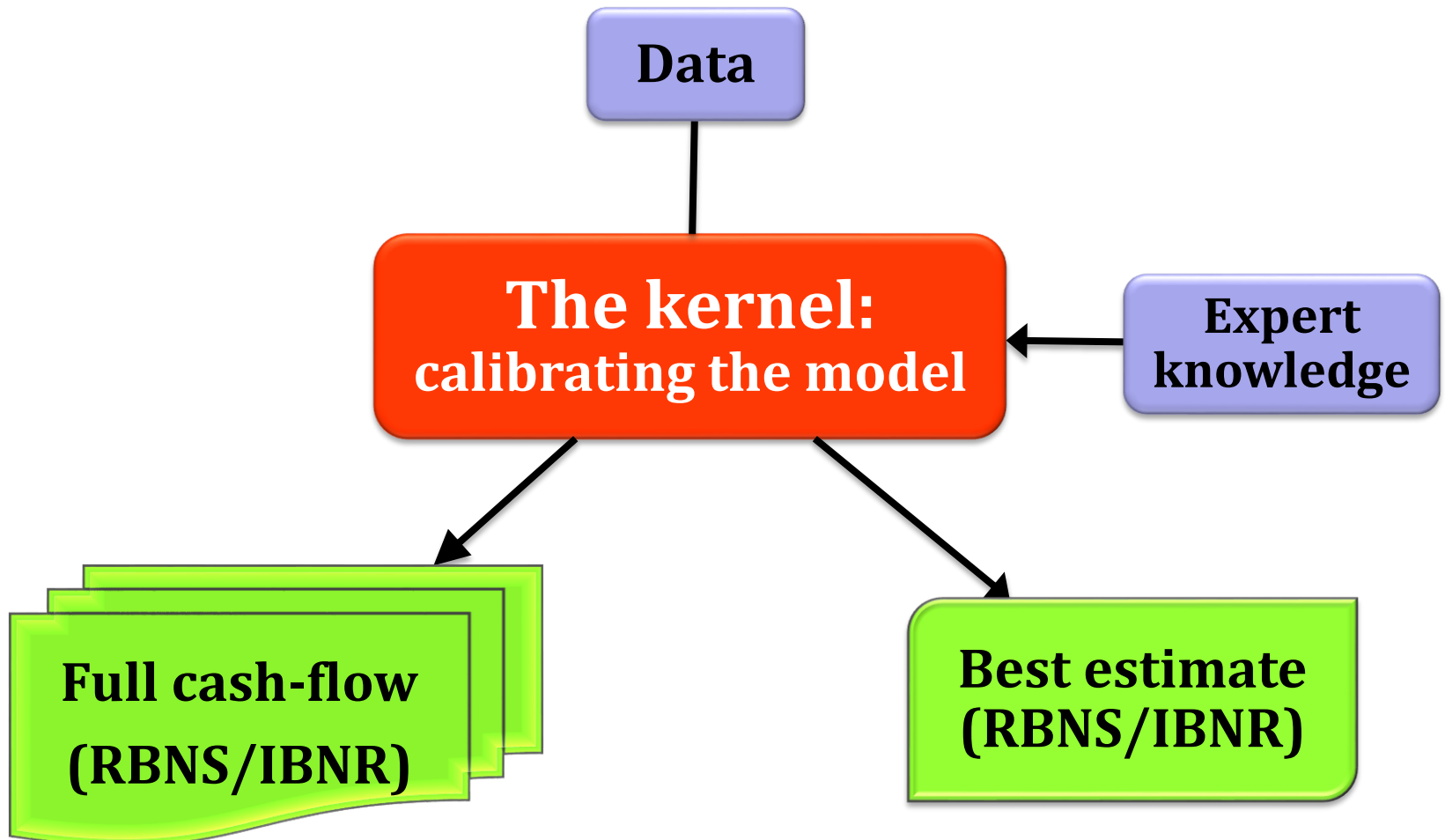
RBNS preserving Double Chain Ladder

Severity inflation





The Double Chain Ladder package





Visualizing the data: the histogram

DEVELOPMENT

ACCIDENT

Payment data

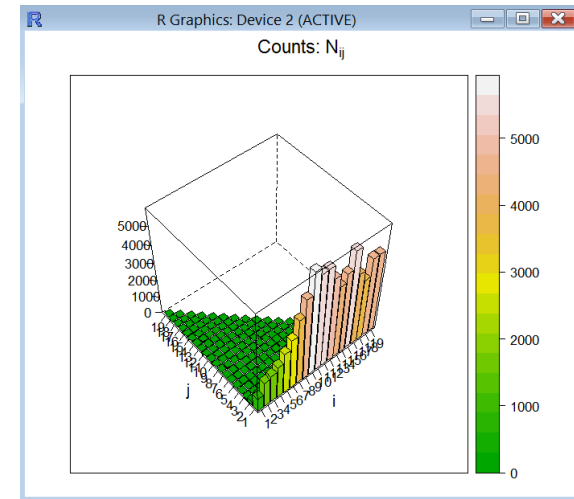
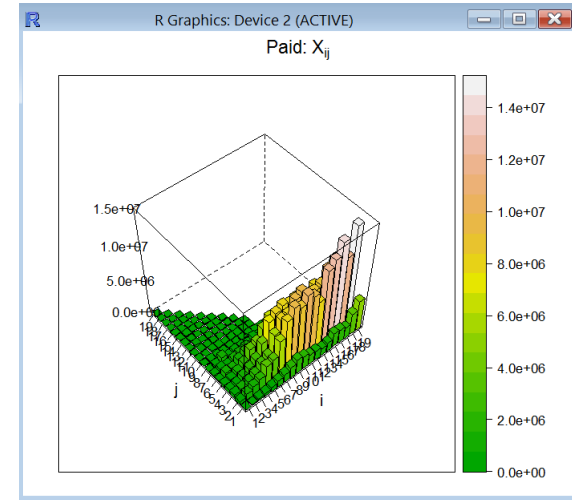
	1	2	3	4	5	6	7
1							
2							
3							
4							
5							
6							
7							

REPORTING

ACCIDENT

Counts data

	1	2	3	4	5	6	7
1							
2							
3							
4							
5							
6							
7							





The kernel: parameter estimation using DCL

- `dcl.estimation()` , `bdcl.estimation()` ,
`idcl.estimation()` , `pdcl.prediction()`

R Documentation

Parameter estimation - Double Chain Ladder model

Description

Compute the estimated parameters in the model (delay parameters, severity underwriting inflation, severity mean and variance) using the Double Chain Ladder method.

Usage

```
dcl.estimation( Xtriangle , Ntriangle , adj = 1 , Tables = TRUE , num.dec = 4 )
```

Arguments

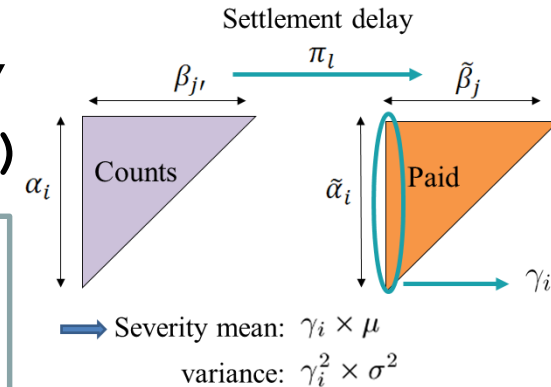
Xtriangle The paid run-off triangle: incremental aggregated payments. It should be a matrix with incremental aggregated payments located in the upper triangle and the lower triangle consisting in missing or zero values.

Ntriangle The counts data triangle: incremental number of reported claims. It should be a matrix with the observed counts located in the upper triangle and the lower triangle consisting in missing or zero values. It should have the same dimension as **Xtriangle** (both in the same aggregation level (quarters, years, etc.))

adj Method to adjust the estimated delay parameters for the distributional model. It should be 1 (default value) or 2. See more in details below.

Tables Logical. If TRUE (default) it is showed a table with the estimated parameters.

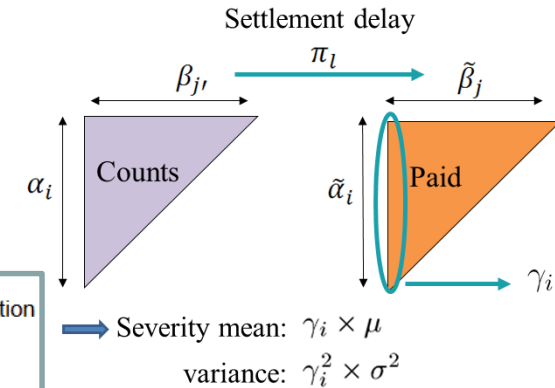
num.dec Number of decimal places used to report numbers in the tables (if **Tables=TRUE**).





The kernel: parameter estimation using DCL

- The function `Plot.dcl.par()` to visualize the break down of the classical chain ladder parameters



Plot.dcl.par {DCL}

R Documentation

Plotting the estimated parameters in the DCL model

Description

Show a two by two plot with the estimated parameters in the Double Chain Ladder model

Usage

```
Plot.dcl.par( dcl.par , type.inflat = 'DCL' )
```

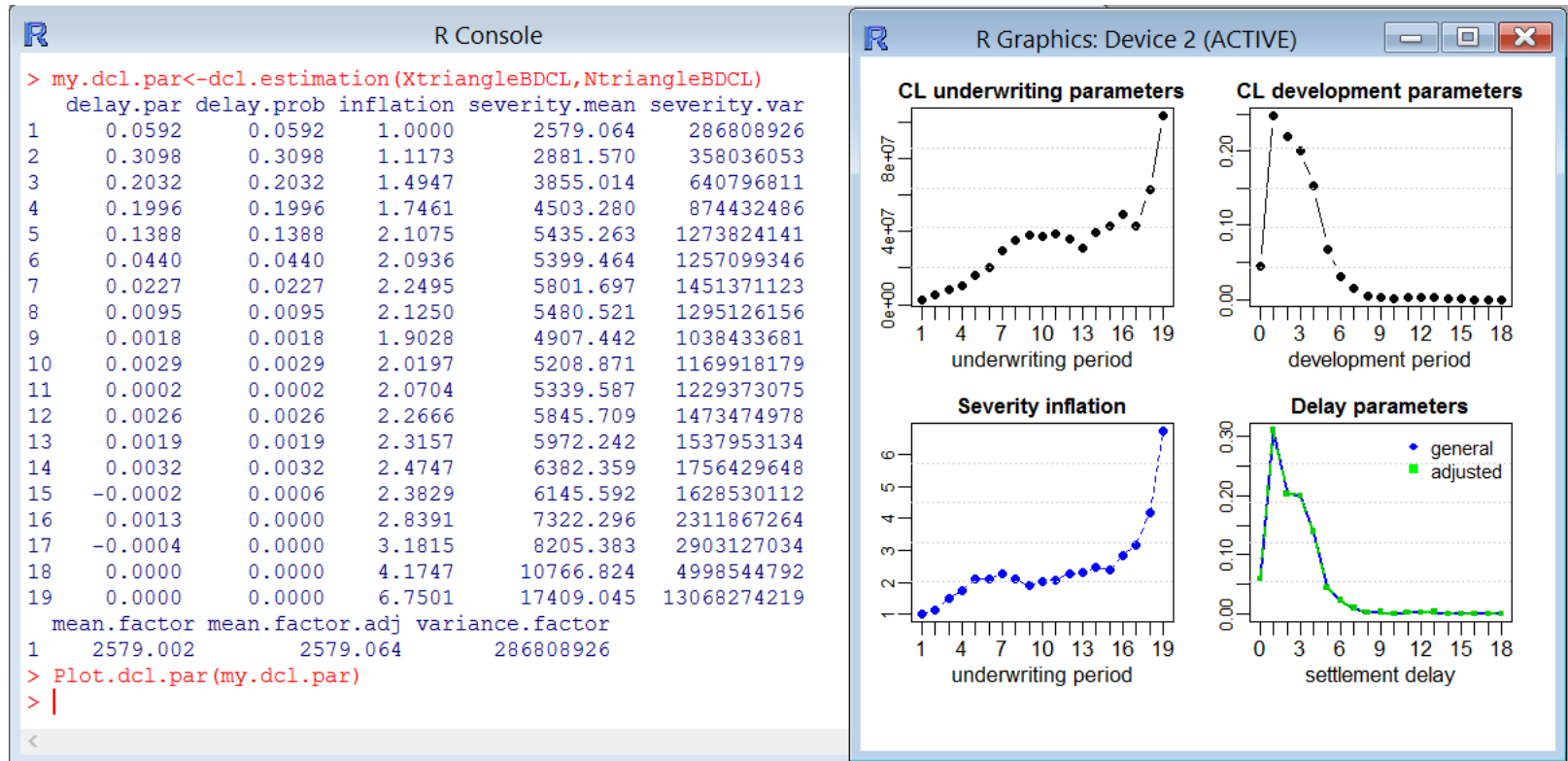
Arguments

`dcl.par` A list object with the estimated parameters: the value returned by the functions `dcl. estimation`, `bdcl. estimation` or `idcl. estimation`.

`type.inflat` Method used to estimate the inflation. Possible values are: 'DCL' (default) if it was used `dcl. estimation`, 'BDCL' if `bdcl. estimation`, and 'IDCL' if `idcl. estimation`



The functions in action: an example



Parameter estimates in two cases: the basic DCL model (only mean specifications) and the distributional model.



The best estimate: RBNS/IBNR split using DCL

□ The function `dcl.predict()`

`dcl.predict` {DCL}

R Documentation

Pointwise predictions (RBNS/IBNR split)

Description

Pointwise predictions by calendar years and rows of the outstanding liabilities. The predictions are splitted between RBNS and IBNR claims.

Usage

```
dcl.predict( dcl.par , Ntriangle , Model = 2 , Tail = TRUE , Tables = TRUE , summ.by="diag", num.dec = 2 )
```

Arguments

`dcl.par` A list object with the estimated parameters: the value returned by the functions `dcl. estimation`, `bdcl. estimation` or `idcl. estimation`.

`Ntriangle` Optional. The counts data triangle: incremental number of reported claims. It should be a matrix with the observed counts located in the upper triangle and the lower triangle consisting in missing or zero values. It should has the same dimension as the `Xtriangle` (both in the same aggregation level (quarters, years, etc.)) used to derive `dcl.par`

`Model` Possible values are 0, 1 or 2 (default). See more details below.

`Tail` Logical. If `TRUE` (default) the tail is provided.

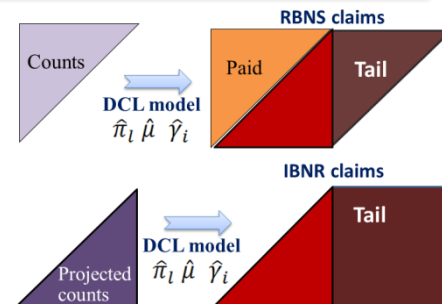
`Tables` Logical. If `TRUE` (default) it is shown a table with the predicted outstanding liabilities in the future calendar periods (`summ.by="diag"`) or by underwriting period (`summ.by="row"`).

`summ.by` A character value such as `"diag"`, `"row"` or `"cell"`.

`num.dec` Number of decimal places used to report numbers in the tables. Used only if `Tables=TRUE`

Details

If `Model=0` or `Model=1` then the predictions are calculated using the DCL model parameters in assumptions M1-M3 (general delay parameters, see Martinez-Miranda, Nielsen and Verrall 2012). If `Model=2` the adjusted delay probabilities (distributional model D1-D4) are considered. By





The full cash-flow: Bootstrapping using DCL

❑ The function `dcl.boot()`

R Documentation

Bootstrap distribution: the full cashflow

Description

Provide the distribution of the IBNR, RBNS and total (RBNS+IBRN) reserves by calendar years and rows using bootstrapping.

Usage

```
dcl.boot( dcl.par , sigma2 , Ntriangle , boot.type = 2 , B = 999 , Tail = TRUE , summ.by = "diag" , Tables = TRUE , num.dec = 2 )
```

Arguments

`dcl.par` A list object with the estimated parameters: the value returned by the functions [dcl.estimate](#), [bdcl.estimate](#) or [idcl.estimate](#).

`sigma2` Optional. The variance of the individual payments in the first underwriting period.

`Ntriangle` The counts data triangle: incremental number of reported claims. It should be a matrix with the observed counts located in the upper triangle and the lower triangle consisting in missing or zero values. It should be the same triangle used to get the value passed by the argument `dcl.par`.

`boot.type` Choose between values 1, to provide only the variance process, or 2 (default), to take into account the uncertainty of the parameters.

`B` The number of simulations in the bootstrap algorithm. The default value is 999.

`Tail` Logical. If TRUE (default) the tail is provided.

`summ.by` A character value such as "diag", "row" or "cell".

`Tables` Logical. If TRUE (default) it is showed a table with the summary (mean, standard deviation, 1%, 5%, 50%, 95%, 99%) of the distribution of the outstanding liabilities in the future calendar periods (if `summ.by="diag"`) or by underwriting period (if `summ.by="row"`).

`num.dec` Number of decimal places used to report numbers in the tables. Used only if `Tables=TRUE`

Details

❑ The function `Plot.cashflow()`



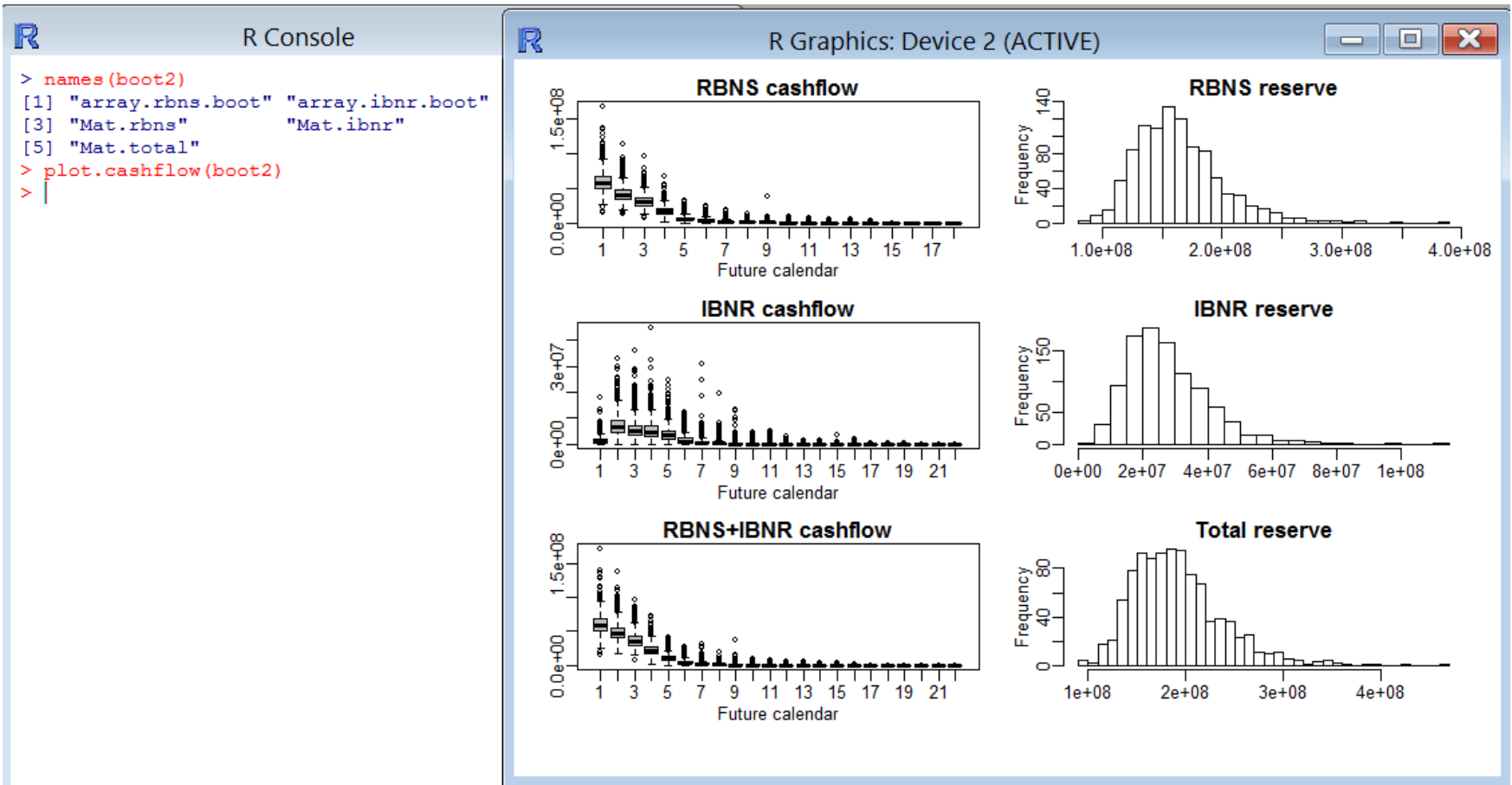
The functions in action: an example

```
R Console
> boot2<-dcl.boot(my.dcl.par,Ntriangle=NtriangleBDCL)
[1] "Please wait, simulating the distribution..."
[1] "Done!"
  period      rbns    mean.rbns    sd.rbns    Q1.rbns    Q5.rbns
1      1 59845052.96 60104639.86 15073076.18 33597995.93 40915229.26
2      2 41447058.01 41679263.34 11015109.71 22154274.56 27730524.16
3      3 31016097.53 31146079.93  9826146.21 14928552.44 18278582.96
4      4 17542089.42 17251007.40  6956163.95  4958809.18  8595612.19
5      5  6443018.76  6403003.15  3843801.59 1016332.33  2071798.34
6      6  3192176.74  3510417.33  2623285.96  177136.11  762954.18
7      7  1445598.60  1597909.78  1873972.33    2517.46  84721.67
8      8    675017.48   852208.53  1174759.22     0.00   412.15
9      9    642274.45   536551.31  1424260.00     0.00     0.00
10     10   423522.65   376713.73   827293.75     0.00     0.00
11     11   535548.94   164627.71   503755.34     0.00     0.00
12     12   404459.01   96801.19   355413.76     0.00     0.00
13     13   334964.95    56962.35  324013.16     0.00     0.00
14     14    60022.99   13651.87  137771.89     0.00     0.00
15     15         0.00     95.42    2144.22     0.00     0.00
16     16         0.00         0.00         0.00     0.00     0.00
17     17         0.00         0.00         0.00     0.00     0.00
18     18         0.00         0.00         0.00     0.00     0.00
19     19         0.00         0.00         0.00     0.00     0.00
20     20         0.00         0.00         0.00     0.00     0.00
21
22
23
24
25
26
27
28
```

- A table showing a summary of the distribution: mean, std. deviation, quantiles.
- Arrays and matrices with the full simulated distributions



The functions in action: an example

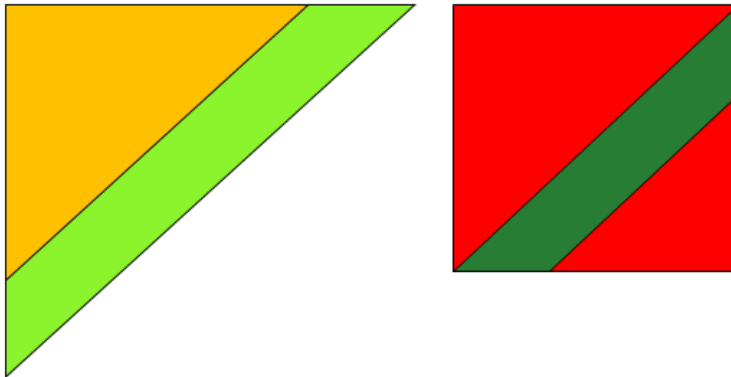




- ❑ The function **validating.incurred()**

Testing results against experience:

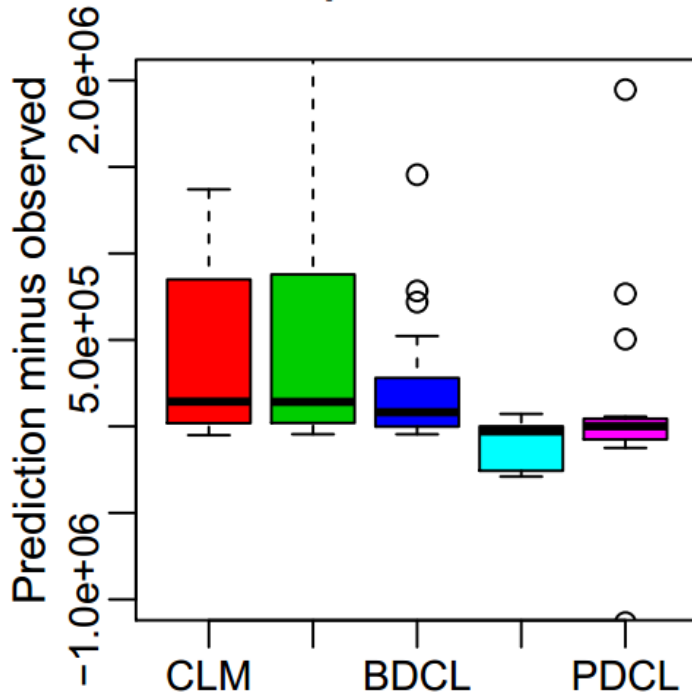
1. Cut $c=1,2,\dots$ diagonals (periods) from the observed triangle.
2. Apply the estimation methods.
3. Compare forecasts and actual values.



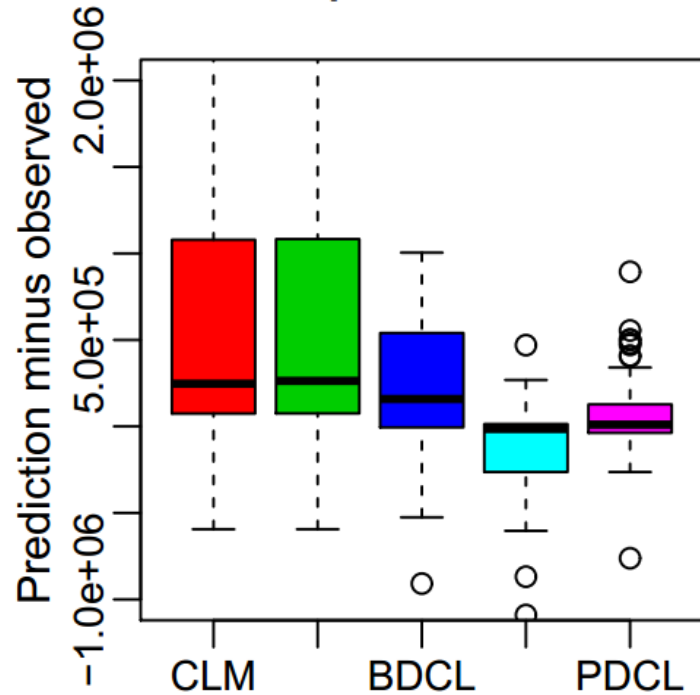


Validation

1 periods cut



4 periods cut





Summary: the content of the package

